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# Microwave dielectric properties and infrared reflectivity spectra analysis of two novel low-firing $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$ (B = Mg, Zn) ceramics with garnet structure

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## Abstract

Two Ag-containing microwave dielectric ceramics  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) with garnet structure were prepared through solid-state reaction method. Dense ceramics were obtained at low sintering temperatures, 665 °C for  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  and 730 °C for  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$ . Their microwave dielectric properties were

characterized for the first time and analyzed by means of packing fraction, bond valence, octahedral distortion, Raman spectra and infrared reflectivity spectra. Both compounds displayed high chemical compatibility with Ag electrodes. Additionally, thermally stable ceramics with near-zero temperature coefficients of resonance frequency ( $\tau_f$ ) were achieved by forming ceramic composites with  $\text{CaTiO}_3$ .

**Keywords:** Ceramics; Garnet structure; Dielectric properties;  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$

## 1. Introduction

Recently, microwave dielectric properties of garnet vanadates  $\text{A}_3\text{B}_2\text{V}_3\text{O}_{12}$  have attracted extensive attention owing to their excellent dielectric performances and the potential applications in the low temperature co-fired ceramics (LTCC) technology. Some garnet vanadates exhibited low sintering temperatures ( $< 960^\circ\text{C}$ ), low dielectric constants ( $\epsilon_r$ ), high quality factors ( $Q \times f$ ), and compositionally adjustable temperature coefficients of resonant frequency ( $\tau_f$ ) [1-8]. In comparison to the Al- and Si-based garnets that have high sintering temperatures ( $> 1300^\circ\text{C}$ ) [9], it is reasonable to propose that the low sintering temperature of garnet vanadates originates from the low melting temperature ( $\sim 690^\circ\text{C}$ ) of vanadium oxide. Thus, it is of great interest to search for novel low-firing microwave dielectric materials from garnet vanadates. Fortunately, the structural complexity of garnet provides great possibilities for composition design with wide range of cations available for A/B sites (A presents an

8-coordinated position while B is an octahedral site) [10-12]. To date, however, the search for low-firing microwave dielectric materials in garnet vanadates is lacking in specific designing guidelines and are almost based on trial and error method. .

Based on the cation occupation in garnets given in supplementary Table S1, it could be summarized that the structural stability of garnet depends strongly on the effective ionic radius of the A-( $r_A$ ) and B-site ( $r_B$ ) cations. A simple conclusion is drawn that the garnet structure can be stabilized when  $0.92 < r_A < 1.51$  and  $0.72 < r_B < 0.76$  [13]. In consideration of the ionic radius of  $\text{Ag}^+$  (1.28 Å) and  $\text{Ca}^{2+}$  (1.12 Å) in A site while  $\text{Mg}^{2+}$  (0.72 Å) and  $\text{Zn}^{2+}$  (0.74 Å) occupying the B site, two garnet compounds  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) were proposed.

Besides, some AgO-rich ceramics have been recently reported with favorable microwave dielectric properties and low sintering temperature, e.g.  $(\text{Na}_{1.2}\text{Ag}_{0.8})\text{MO}_4$  sintered at 410 °C with  $\epsilon_r = 8.1$ ,  $Q \times f = 44,800$  GHz and  $\tau_f = -82$  ppm/°C,  $(\text{AgBi})_{0.5}\text{WO}_4$  sintered at 580 °C with  $\epsilon_r = 35.9$ ,  $Q \times f = 13,000$  GHz and  $\tau_f = -69$  ppm/°C [14,15]. Therefore, it is expected that the proposed  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics might exhibit low sintering temperatures and good dielectric properties.

In this paper,  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics were prepared by the solid-state reaction methods. The microwave dielectric properties were characterized for the first time, and the structure and properties were investigated by means of packing fraction, bond valence, octahedral distortion, Raman spectra and infrared reflectivity spectra. Furthermore, the adjustment for the temperature coefficients of resonant frequency ( $\tau_f$ ) of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics were also studied by

the addition of  $\text{CaTiO}_3$  [16].

## 2. Experimental procedure

High-purity raw powders  $\text{Ag}_2\text{O}$ ,  $\text{CaCO}_3$ ,  $\text{ZnO}$ ,  $\text{MgO}$ , and  $\text{NH}_4\text{VO}_3$  (>99.0%, Guo-Yao Co. Ltd., Shanghai, China) were weighed according to the stoichiometry and ball-milled in alcohol medium for 4 h. After drying, calcination was carried out at 600 °C for 4 h in air. Subsequently, the calcined powders were re-milled for 4 h and polyvinyl alcohol (PVA) was added as a binder. The resultant powders were pressed into disks with 10 mm in diameter and 5-6 mm in height by uniaxial pressing under a pressure of 80 MPa. The green disks were heated to 550 °C for 2 h at a heating rate of 1.5 °C /min to remove the PVA. Finally, these specimens were sintered at various temperatures for 4 h.

X-ray diffraction (XRD) data collected by an X-ray diffractometer ( $\text{CuK}\alpha 1$ , 1.54059 Å, Model X'Pert PRO, PANalytical, Almelo, Holland) were used to identify phase purity. Rietveld refinements using FULLPROF were performed to analyze crystal structure. The apparent densities of the sintered ceramics were measured by the Archimedes' method. The microstructural images of the polished and thermally etched samples were recorded using a scanning electron microscope (SEM) (Model JSM6380-LV SEM, Jeol, Tokyo, Japan). In thermal etching, all samples were heated at 50°C below their sintering temperatures for 10 minutes. Composition analysis were performed using energy-dispersive spectroscopy (EDS, IE 350; INCA, Oxford, U.K.). The Raman spectra were recorded at room temperature by using a Raman spectrometer (Thermo Fisher Scientific DXR, America) with a 532 nm line in the

range of 100-1000  $\text{cm}^{-1}$ . The permittivity and dielectric loss of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ceramics were measured in the  $\text{TE}_{011}$  mode by Hakki and Coleman method [17] using the network analyzer (Model N5230A, Agilent Co., Palo Alto, California) at the frequency range of 10 MHz-40 GHz. The  $\tau_f$  values were analyzed using a temperature chamber (Delta 9039, Delta Design, San Diego, CA) and calculated using the following equation:

$$\tau_f = \frac{f_2 - f_1}{f_1 (T_2 - T_1)} \quad (1)$$

where,  $f_1$  and  $f_2$  were the resonant frequency of the dielectric resonator at temperature 25 °C and 85 °C, respectively.

Room-temperature infrared reflectivity spectra were measured using a Bruker IFS 66v FT-IR spectrometer (Bruker Optics, Ettlingen, Germany) on the infrared beam line station (U4) at the National Synchrotron Radiation Lab (NSRL), China. The infrared reflectivity spectra were analyzed by the harmonic oscillator model as follow:

$$\varepsilon^*(\omega) = \varepsilon_\infty + \sum_{j=1}^n \left( \frac{\omega_{pj}^2}{\omega_{oj}^2 - \omega^2 - j\gamma_j\omega} \right) \quad (2)$$

where  $\varepsilon^*(\omega)$  is the complex dielectric function,  $\varepsilon_\infty$  is the dielectric constant caused by the electronic polarization at high frequencies,  $\gamma_j$ ,  $\omega_{oj}$  and  $\omega_{pj}$  are the damping factor, the transverse frequency, and plasma frequency of the  $j$ -th Lorenz oscillator, respectively, and  $n$  is the number of transverse phonon modes. The complex reflectivity  $R(\omega)$  can be written as:

$$R(\omega) = \left| \frac{1 - \sqrt{\varepsilon^*(\omega)}}{1 + \sqrt{\varepsilon^*(\omega)}} \right|^2 \quad (3)$$

### 3. Results and discussion

Fig. 1(a) shows XRD patterns of the  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Mg}, \text{Zn}$ ) samples sintered at 665 °C and 730 °C, respectively. The peak positions obtained from the standard JCPDS cards (No. 024-1038 and No. 050-0393) are also given for indexing. By comparison, all the peaks matched well with the standard peaks, indicating single phase with cubic garnet structure in a space group of Ia-3d (230) was formed. Fig. 1(b) shows XRD pattern, SEM image, and EDS of the co-fired  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  with 20 wt% silver sintered at 730 °C as a representative. Only the peaks of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  and Ag were detected in the XRD patterns. SEM micrograph exhibited some larger Ag grains ( $\sim 4\text{-}6\ \mu\text{m}$ ) distributed randomly among the  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  matrix with smaller grains, further identified by the EDS analysis. Similar results were confirmed for the  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  matrix. These results confirm that the  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ceramics are chemically compatible with silver electrodes at the sintering temperatures. To further confirm the phase purity and study their structural difference, Rietveld refinements using Fullprof software were performed based on the XRD data sets. The observed and calculated patterns are shown in Fig. 2 (a) and (b). Refinement data and crystal parameters are listed in Table 1. The good match with low residual factors confirm the reliability of the refinement. Schematic crystal structure of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  are shown in Fig. 2 (c) and (d). Mg and Zn cations occupy the  $[\text{BO}_6]$  octahedral, while V cations are coordinated by four oxygen atoms, thus forming  $[\text{VO}_4]$  tetrahedra. The neighboring tetrahedra and octahedral interconnect by corner-sharing, forming dodecahedra where A ions are located. As shown in Fig. 2 (d), Zn-O bond lengths are much longer in comparison to the Mg-O band, and the distortion of  $[\text{ZnO}_6]$  octahedral

$101.3 \pm 0.1$  is more evident than that of  $[\text{MgO}_6]$   $36.8 \pm 0.1$  with different B-O bond lengths and O-B-O band angles.

The bulk densities and relative densities of the  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Mg}, \text{Zn}$ ) ceramics sintered at various temperatures are shown in Fig. 3. As the sintering temperature increased, the density of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  increased to a maximum value of  $3.70 \pm 0.01 \text{ g/cm}^3$  ( $\sim 95.7 \pm 0.2 \%$  of the theoretical density) at  $730^\circ\text{C}$ , whereas the density decreased slightly with the further increases of sintering temperature.  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  exhibited a similar variation in density with sintering temperature, and the sample sintered at  $665^\circ\text{C}$  yielded the highest bulk density of  $4.26 \pm 0.01 \text{ g/cm}^3$  that is  $94.2 \pm 0.2 \%$  of the theoretical density.

Fig. 4 (a-e) shows the SEM images recorded on the polished and thermally etched surfaces of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  ceramics sintered at different temperatures. As seen in Fig. 4(a), some visible pores were observed, which is consistent with the relatively low density of the ceramics sintered at  $675^\circ\text{C}$ . The microstructure became denser as the sintering temperature increased while no significant change in the average grain size ( $1\sim 2\mu\text{m}$ ) was detected from  $675$  to  $730^\circ\text{C}$ . However, abnormal grain growth was observed with further increase in sintering temperature to  $745^\circ\text{C}$ , characterized by large grains ( $\sim 100 \mu\text{m}$ ) and cotton-shaped grains. This might be the consequence of liquid phase sintering at elevated temperatures which is related to the local composition heterogeneity. A homogeneous microstructure with average grain size about  $1\text{-}3\mu\text{m}$  was developed when the ceramics were sintered at  $730^\circ\text{C}$ . As



shown in Fig. 4(f), a dense microstructure with closely packed grains was obtained in the  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramic sintering at 665 °C.

The room-temperature Raman spectra of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics are shown in Fig. 5. For the cubic garnet structure with a space group Ia-3d, the Raman activities can be summarized based on the group theory as follows:

$$\Gamma_{\text{optic}} = 3 A_{1g} + 9 E_g + 16 T_{2g} \quad (4)$$

The vibrational models of  $\text{A}_3\text{B}_2\text{V}_3\text{O}_{12}$  were reported to be divided into internal and external parts [18-20]. The internal vibrations were mainly assigned for the vibration of  $[\text{VO}_4]^{3-}$  tetrahedron, whereas the external vibration contributed to the translational motion of cations and  $[\text{VO}_4]^{3-}$ . As observed, 16 emission bands fitted by the Gaussian-Lorentzian mode were detected. Below 250  $\text{cm}^{-1}$ , the models were associated with the external translational motions of  $\text{Ag}^+$  and  $\text{Ca}^{2+}$  cations. In the range of 250-470  $\text{cm}^{-1}$ , the Raman models were assigned for the rotational and translational motions of  $[\text{VO}_4]^{3-}$ . The peaks at the 500-800  $\text{cm}^{-1}$  were ascribed to the bending vibration of  $[\text{VO}_4]^{3-}$ . The Raman models between 800 and 900  $\text{cm}^{-1}$  were assigned for the asymmetric stretching vibration of  $(\text{VO}_4)^{3-}$  unit. The modes 909 and 931  $\text{cm}^{-1}$  for  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  and 919 and 930  $\text{cm}^{-1}$  for  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  modes were related to the symmetric stretching of the  $(\text{VO}_4)^{3-}$  unit [21]. The different amounts Raman modes in the  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  systems can be explained by the different ionic radii of B-site cations and the overlapping of the Raman peaks.

The variations in the microwave dielectric properties ( $\epsilon_r$ ,  $Q \times f$ , and  $\tau_f$ ) of the  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics as a function of the sintering temperature are

shown in Fig. 6. It was found that both relative permittivity and quality factor exhibited slight dependence on the sintering temperature, similar to the variation tendency of the apparent density. However, the  $\tau_f$  values did not significantly change as the sintering temperature increased. The optimum microwave dielectric properties were obtained with  $\epsilon_r = 10.28 \pm 0.1$ ,  $Q \times f = 43,000 \pm 2000$  GHz and  $\tau_f = -69 \pm 2.0$  ppm/°C for  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  at the sintering temperature of 730 °C and  $\epsilon_r = 11.15 \pm 0.1$ ,  $Q \times f = 26,930 \pm 1500$  GHz,  $\tau_f = -95 \pm 2.5$  ppm/°C for  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  sintered at the 665 °C.

It is well known that the microwave dielectric performances are influenced by the intrinsic factors, e.g. ionic polarizability, the anharmonic terms in the crystal's potential energy and the extrinsic factors related to densification, impurity, second phases and the lattice defects [5, 22]. As evidenced by the XRD analysis, the effects from impurity and second phases could be neglected. The dependence of dielectric properties manifests that the densification plays a crucial role in affecting the dielectric permittivity. In order to eliminate the contribution from the densification, the relative permittivity was corrected by the porosity-correction equation proposed by Bosman and Having [23, 24]. The corrected  $\epsilon_r$  values, shown in Fig.6 (a), exhibit weak dependence on sintering temperature and fluctuate around  $\sim 10.7 \pm 0.1$  for  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  and  $\sim 11.6 \pm 0.1$  for  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$ . By comparison, the  $\epsilon_r$  of  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  is slightly higher than its Mg counterpart, which might be due to the higher ionic polarization of  $\text{Zn}^{2+}$  ( $2.04 \text{ \AA}^3$ ) than  $\text{Mg}^{2+}$  ( $1.32 \text{ \AA}^3$ ) based on the Clausius-Mosotti equation [14, 25]. On the other hand,  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  possessed a

much higher  $Q \times f$  value compared to  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$ , which might be partly related to the lower relative density of as-sintered  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramics. In addition, the intrinsic loss can be reflected in terms of packing fraction. Generally, it is proposed that the increase in the packing fraction leads to a decrease in the lattice vibration, which then results in the decrease of intrinsic losses [26-29]. As exhibited in Table 1, the calculated packing fraction of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Mg}, \text{Zn}$ ) is  $66.8 \pm 0.01\%$  and  $66.6 \pm 0.01\%$ , respectively. Thus, the higher  $Q \times f$  value of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  could be partly related to the higher packing fraction.

The bond valences of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Mg}, \text{Zn}$ ) with the general formula of  $\text{A}_3\text{B}_2\text{V}_3\text{O}_{12}$  are shown in Table 1 calculated using the following equations:

$$V_i = \sum_j V_{ij} \quad (5)$$

$$V_{ij} = \exp \left[ \frac{R_{ij} - d_{ij}}{b} \right] \quad (6)$$

Where  $R_{ij}$  is the bond valence parameter,  $d_{ij}$  is the length of a bond between atoms  $i$  and  $j$ , and  $b$  is a universal constant ( $0.37 \text{ \AA}$ ) [30]. The bond valence of  $V_B$  and  $V_O$  are listed in Table 2. The larger  $\tau_f$  value of  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  might be ascribed to the smaller bond valence of  $V_B$  and  $V_O$  compared to those of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$ . Similar results were obtained in  $\text{Ba}(\text{Co}_{1-x}\text{Mg}_x)_2(\text{VO}_4)_2$  [31],  $\text{LiMoVO}_6$  [32] and  $\text{Bi}_2\text{O}_3\text{-TiO}_2\text{-V}_2\text{O}_5$  system [33].

As the  $\tau_f$  values of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Mg}, \text{Zn}$ ) ceramics are too large for practical application, efforts were carried out to improve the temperature stability of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  by forming composite ceramics with  $\text{CaTiO}_3$  with a large positive  $\tau_f$  value  $\sim +800 \text{ ppm/}^\circ\text{C}$ . The results are shown in Table 2 and a near-zero temperature

coefficient of resonant frequency ( $\tau_f$ )  $\sim -2 \pm 0.2$  ppm/ $^{\circ}\text{C}$  was achieved in 0.91AgCa<sub>2</sub>Mg<sub>2</sub>V<sub>3</sub>O<sub>12</sub>-0.09CaTiO<sub>3</sub> ceramic, along with  $\epsilon_r \sim 13.78 \pm 0.1$  and  $Q \times f \sim 30,700 \pm 1600$  GHz. The 0.88AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub>-0.12CaTiO<sub>3</sub> sintering at 725  $^{\circ}\text{C}$  resulted in  $\epsilon_r \sim 15.89 \pm 0.1$ ,  $Q \times f \sim 19,600 \pm 1200$  GHz and a near-zero temperature coefficient of resonant frequency  $\tau_f \sim +1 \pm 0.2$  ppm/ $^{\circ}\text{C}$ .

Based on the classic harmonic oscillator model, the infrared reflectivity spectra were fitted to speculate the intrinsic microwave dielectric properties of AgCa<sub>2</sub>B<sub>2</sub>V<sub>3</sub>O<sub>12</sub> (B = Mg, Zn) ceramics. The fitting results are shown in the Fig. 7 and Table 3. The dielectric permittivity at the high frequencies ( $\epsilon_{\infty}$ ) were  $2.41 \pm 0.05$  and  $2.26 \pm 0.05$ , and the extrapolated values ( $\epsilon_0$ ) were  $7.47 \pm 0.1$  and  $9.52 \pm 0.1$  for AgCa<sub>2</sub>Mg<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub>, respectively, which were lower than the measured ones using the TE<sub>011</sub> method. It suggests that most of the dielectric contribution within microwave region was attributed to the absorptions of phonon oscillations in the infrared region.

The theoretical quality factor values of AgCa<sub>2</sub>B<sub>2</sub>V<sub>3</sub>O<sub>12</sub> (B = Mg, Zn) can also be evaluated from the infrared reflectivity spectra by using the Lorentzian function [34, 35]. In the microwave frequency region ( $\omega \ll \omega_{pj}$ ), the dielectric losses ( $\tan \delta$ ) can be calculated by the following equation:

$$\epsilon' = \epsilon_{\infty} + \sum_{j=1}^n \frac{\omega_{pj}^2}{\omega_{oj}^2} = \epsilon_{\infty} + \sum_{j=1}^n \Delta\epsilon_j \quad (7)$$

$$\tan \delta(\omega) = \frac{\epsilon''}{\epsilon'} = \omega \sum_{j=1}^n \frac{\Delta\epsilon_j \gamma_j}{\omega_{oj}^2 (\epsilon_{\infty} + \sum_{j=1}^n \Delta\epsilon_j)} \quad (8)$$

The theoretical  $Q \times f$  value is  $75,070 \pm 3000$  GHz ( $f = 12.08 \pm 0.1$  GHz) for AgCa<sub>2</sub>Mg<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and  $58,970 \pm 3000$  GHz ( $f = 11.77 \pm 0.1$  GHz) for AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub>.

These values are much higher than the measured ones using the  $TE_{011}$  method. The large deviation between the theoretical and experimental quality factors is due to the adverse influences from the extrinsic factors, such as density, secondary phase, grain size, etc. On the other hand, the fitting results give the optimum quality factor of  $AgCa_2Mg_2V_3O_{12}$  ceramics and offer the possibility to further improve their  $Q \times f$  values by optimizing the experimental processes to minimize extrinsic loss.

#### 4. Conclusions

In this paper,  $AgCa_2B_2V_3O_{12}$  ( $B = Mg, Zn$ ) ceramics with garner structure were prepared by the conventional solid-state reaction method. The phase purity, crystal structure, packing fraction, bond valence, octahedral distortion and microwave dielectric properties were investigated. Raman and infrared reflectivity spectra were original to performing on the  $AgCa_2B_2V_3O_{12}$  ( $B = Mg, Zn$ ) ceramics. Excellent microwave dielectric properties were obtained in  $AgCa_2Mg_2V_3O_{12}$  ceramic sintered at  $730\text{ }^\circ\text{C}$  for 4 h, with a permittivity of  $10.28 \pm 0.1$ ,  $Q \times f$  values  $43,000 \pm 2000\text{ GHz}$ , and a stable  $\tau_f$  values around  $-69 \pm 2.0\text{ ppm}/^\circ\text{C}$ . The  $AgCa_2Mg_2V_3O_{12}$  ceramic sintered at  $665\text{ }^\circ\text{C}$  for 4 h also exhibited an excellent microwave dielectric properties with a  $\epsilon_r \sim 11.15 \pm 0.1$ ,  $Q \times f \sim 26,930 \pm 1500\text{ GHz}$  and  $\tau_f \sim -95 \pm 2.5\text{ ppm}/^\circ\text{C}$ . From the XRD, SEM and EDS analysis, the  $AgCa_2X_2V_3O_{12}$  ceramics showed good chemical compatibility with Ag electrode, which makes it a promising candidate for LTCC application. Additionally, the temperature stability of  $AgCa_2B_2V_3O_{12}$  were adjusted by forming composite ceramics with  $CaTiO_3$ . A near-zero temperature coefficient of resonant frequency ( $\tau_f$ )  $\sim -2 \pm 0.2$  and  $+1 \pm 0.2\text{ ppm}/^\circ\text{C}$  were achieved in the

$0.91\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}-0.09\text{CaTiO}_3$  and  $0.88\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}-0.12\text{CaTiO}_3$  ceramics, respectively.

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## Figure Captions

**Fig. 1** X-ray diffraction patterns of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (a), Backscattered electron image micrograph, and EDS analysis of the  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  ceramic with 20 wt% silver powder (b).

**Fig. 2** The Rietveld refined patterns of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  (a),  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  (b), the structure diagram of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (c), and units  $[\text{BO}_6]$  octahedron and  $[\text{VO}_4]$  tetrahedral of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) (d).

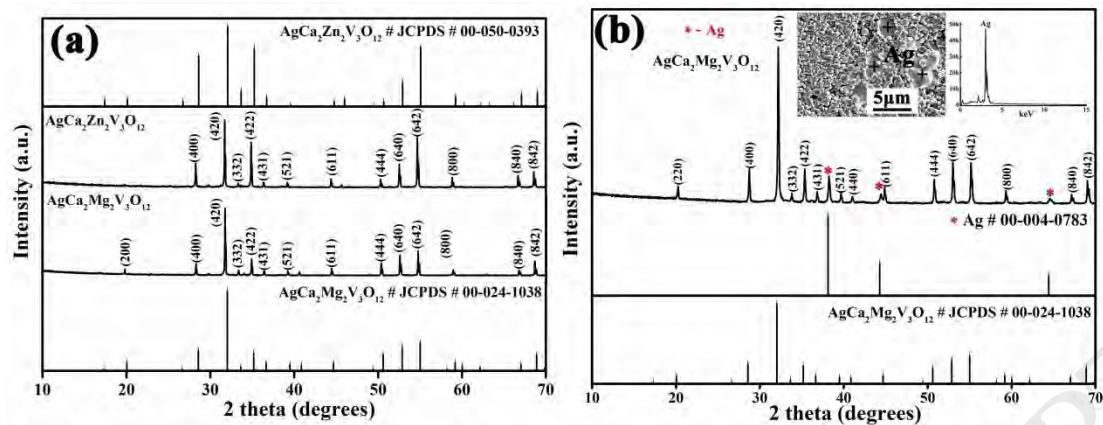
**Fig. 3** The bulk and relative density of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  and  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramics sintering at various temperatures.

**Fig. 4** The SEM images of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  ceramics sintered at 675 °C (a), 690 °C (b), 705 °C (c), 730 °C (d), 745 °C (e) and  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramic sintered at best temperature 665 °C (f) for 4 h.

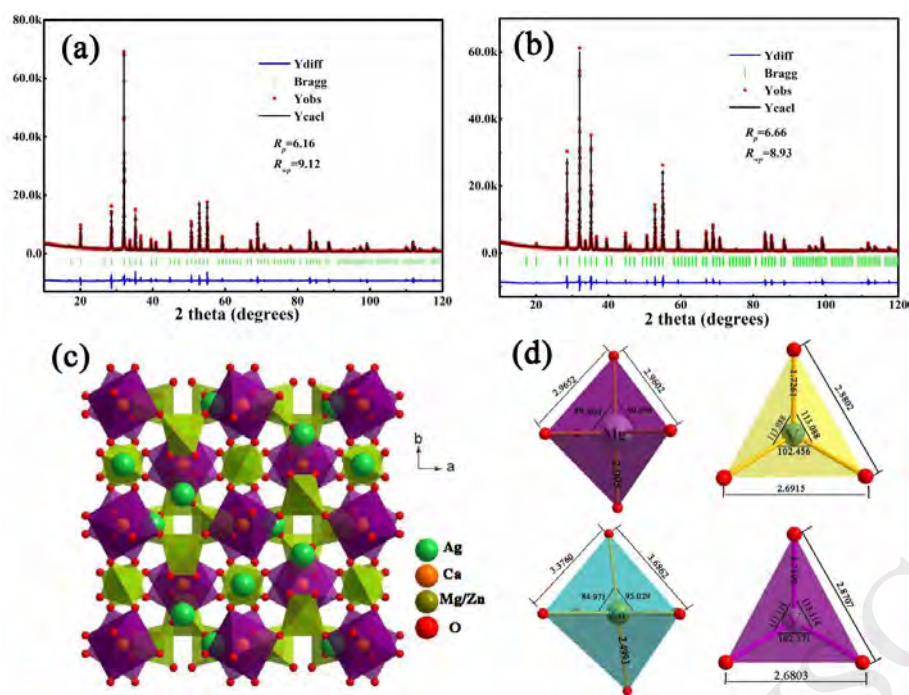
**Fig. 5** The measured and fitted Raman spectra of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics. The hollow red circles are measured values. Solid line represents the fitted values and the dashed line is the Gaussian-Lorentzian mode fitting.

**Fig. 6** The microwave dielectric properties ( $\epsilon_r$ ,  $Q \times f$ , and  $\tau_f$ ) of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  and  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramics as a function of the sintering temperature.

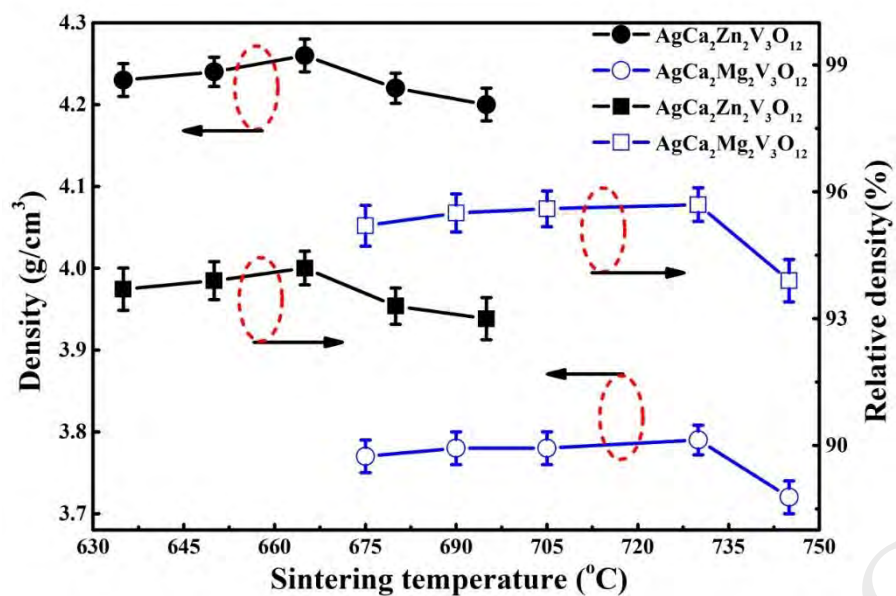
**Fig. 7** Measured and calculated infrared reflectivity spectra and complex dielectric spectra of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) ceramics (solid for fitting values and hollow symbol for measured values).



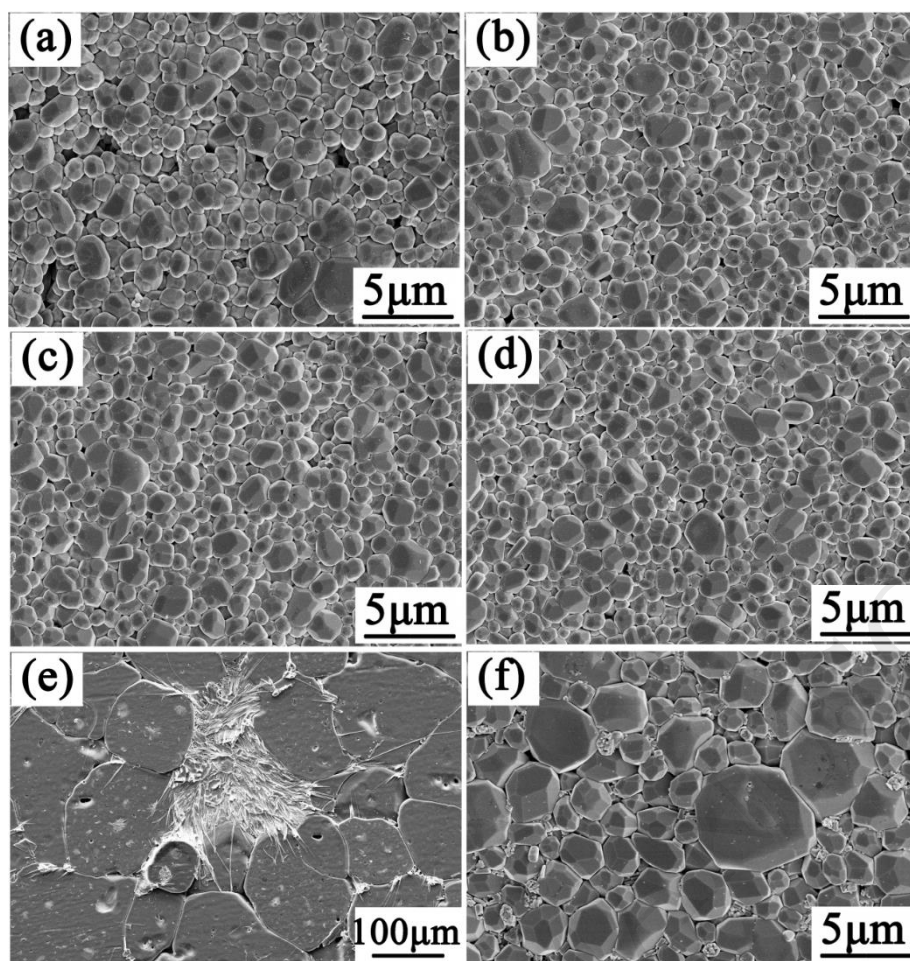
**Fig. 1** (a) X-ray diffraction patterns of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Zn}, \text{Mg}$ ), (b) XRD, Backscattered electron image micrograph, and EDS analysis of the  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  ceramic with 20 wt% silver powder.



**Fig. 2** The Rietveld refined patterns of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  (a),  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  (b), the structure diagram of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (c), and units  $[\text{BO}_6]$  octahedron and  $[\text{VO}_4]$  tetrahedral of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn) (d).

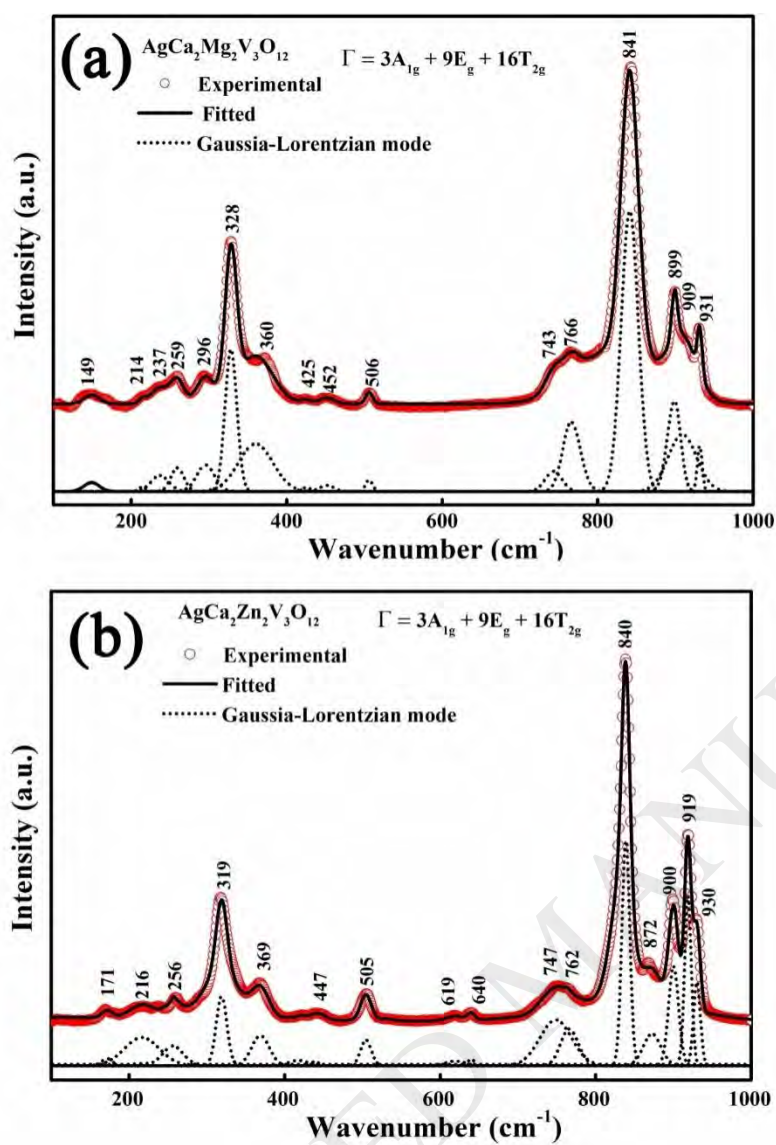


**Fig. 3** The bulk and relative density of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  and  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramics sintering at various temperatures.

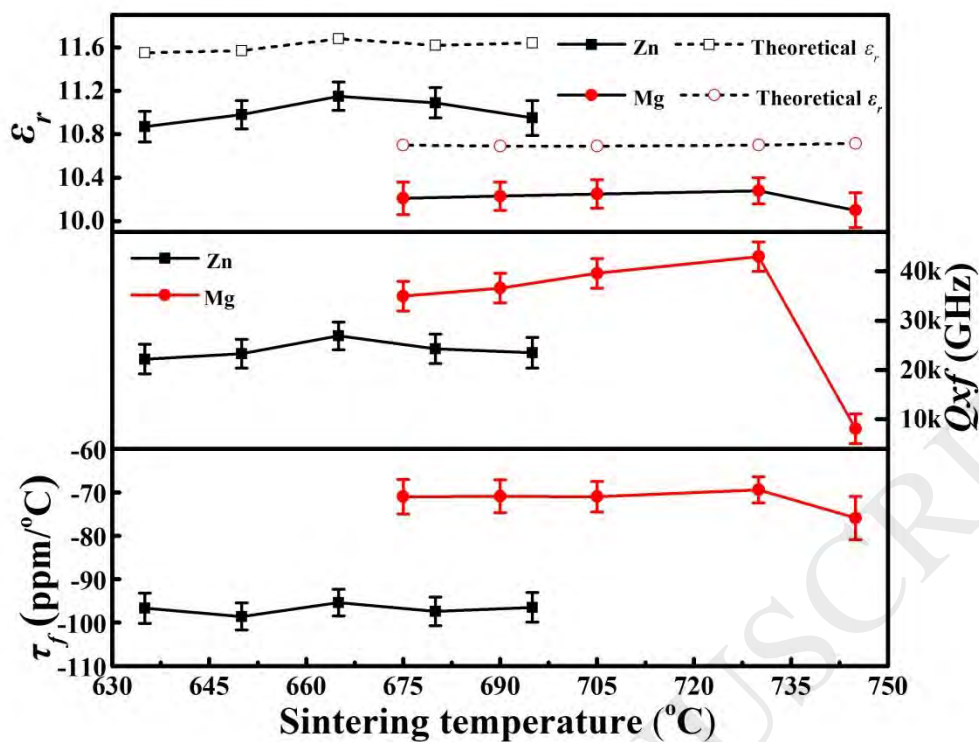


**Fig. 4** The SEM images of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  ceramics sintered at 675 °C (a), 690 °C (b), 705 °C (c), 730 °C (d), 745 °C (e) and  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramic sintered at best temperature 665 °C (f) for 4 h.

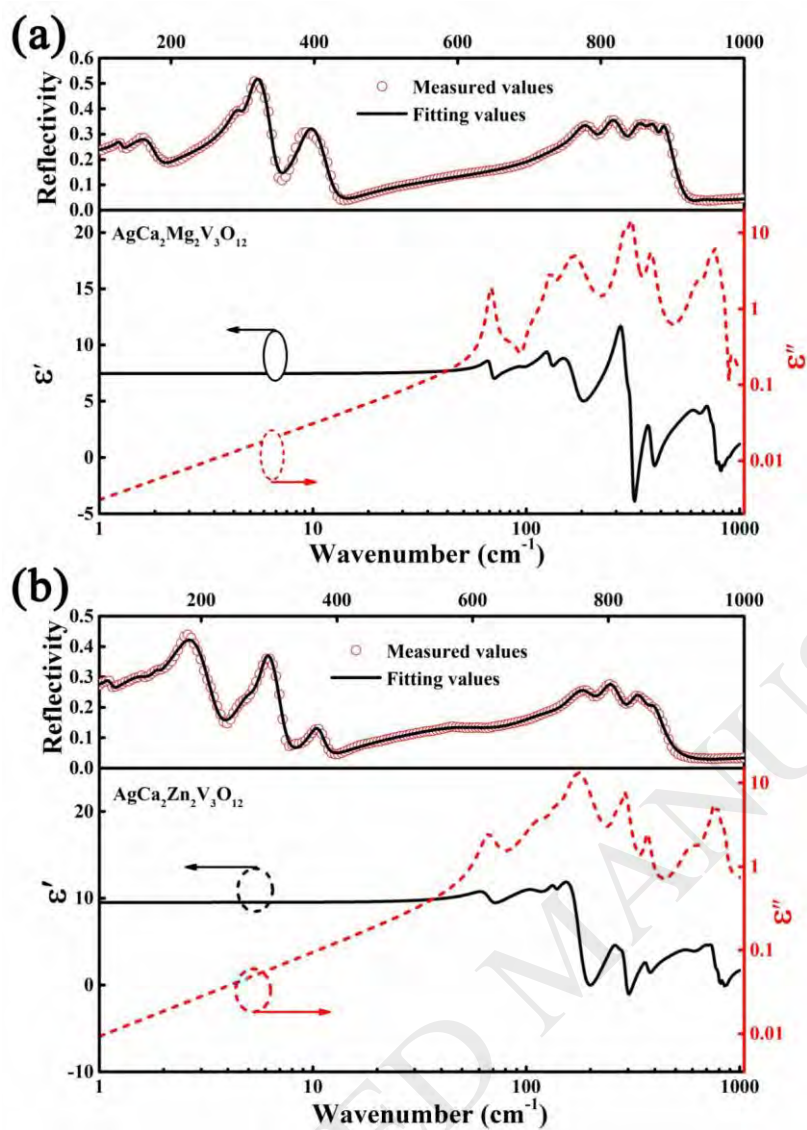




**Fig. 5** The measured and fitted Raman spectra of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $B = \text{Mg}, \text{Zn}$ ) ceramics. The hollow red circles are measured values. Solid line represents the fitted values and the dashed line is the Gaussian-Lorentzian mode fitting.



**Fig. 6** The microwave dielectric properties ( $\epsilon_r$ ,  $Q \times f$ , and  $\tau_f$ ) of  $\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$  and  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$  ceramics as a function of the sintering temperature.



**Fig. 7** Measured and calculated infrared reflectivity spectra and complex dielectric spectra of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  ( $\text{B} = \text{Mg}, \text{Zn}$ ) ceramics (solid for fitting values and hollow symbol for measured values).

**Tables:**

Table 1 The Rietveld refinement dates, packing fraction and bond valence of  $\text{AgCa}_2\text{B}_2\text{V}_3\text{O}_{12}$  (B = Mg, Zn)

Compounds	a (Å)	V (Å <sup>3</sup> )	R <sub>p</sub> (%)	R <sub>wp</sub> (%)	$\rho$ (theoretical) (g/cm <sup>3</sup> )	Packing fraction (%)	V <sub>B</sub> (Å)	V <sub>O</sub> (Å)
$\text{AgCa}_2\text{Mg}_2\text{V}_3\text{O}_{12}$	12.4688 ± 0.0002	1938.54 ± 0.01	6.16 ± 0.01	9.12 ± 0.01	3.960 ± 0.001	66.8 ± 0.01	2.061 ± 0.001	1.999 ± 0.001
$\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$	12.4943 ± 0.0002	1950.43 ± 0.01	6.66 ± 0.01	8.93 ± 0.01	4.492 ± 0.001	66.6 ± 0.01	1.981 ± 0.001	1.955 ± 0.001

Table 2 Microwave dielectric properties of (1-x) AgCa<sub>2</sub>B<sub>2</sub>V<sub>3</sub>O<sub>12</sub> - xCaTiO<sub>3</sub> (B = Mg, Zn)

composite ceramics

Composition	x value	S.T. (°C)	$\epsilon_r$	$Q \times f$ (GHz)	$\tau_f$ (ppm/°C)
AgCa <sub>2</sub> Mg <sub>2</sub> V <sub>3</sub> O <sub>12</sub>	0	730	$10.28 \pm 0.1$	$43,000 \pm 2000$	$-69.4 \pm 2.0$
	0.03	750	$11.56 \pm 0.1$	$39,850 \pm 1800$	$-44.1 \pm 1.5$
	0.06	780	$12.63 \pm 0.1$	$36,800 \pm 1700$	$-20.7 \pm 1.0$
	0.09	820	$13.78 \pm 0.1$	$30,700 \pm 1600$	$-2.4 \pm 0.2$
	0.12	860	$14.40 \pm 0.1$	$27,600 \pm 1500$	$+28.8 \pm 1.1$
AgCa <sub>2</sub> Zn <sub>2</sub> V <sub>3</sub> O <sub>12</sub>	0	665	$11.15 \pm 0.1$	$26,930 \pm 1500$	$-95.4 \pm 2.5$
	0.04	680	$12.47 \pm 0.1$	$24,960 \pm 1400$	$-61.2 \pm 2.0$
	0.08	700	$14.56 \pm 0.1$	$23,200 \pm 1300$	$-27.0 \pm 1.1$
	0.12	725	$15.89 \pm 0.1$	$19,600 \pm 1200$	$+1.3 \pm 0.2$
	0.16	780	$18.05 \pm 0.1$	$17,400 \pm 1000$	$+44.1 \pm 1.5$

Table 3 Phonon parameters obtained from the fitting of infrared reflectivity spectra of

AgCa<sub>2</sub>B<sub>2</sub>V<sub>3</sub>O<sub>12</sub> (B = Mg, Zn)

AgCa <sub>2</sub> Mg <sub>2</sub> V <sub>3</sub> O <sub>12</sub>					AgCa <sub>2</sub> Zn <sub>2</sub> V <sub>3</sub> O <sub>12</sub>				
Mode	$\omega_{oj}$	$\omega_{pj}$	$\gamma_j$	$\Delta\epsilon_j$	Mode	$\omega_{oj}$	$\omega_{pj}$	$\gamma_j$	$\Delta\epsilon_j$
1	68.37	26.58	6.50	0.15	1	66.85	38.19	13.47	0.33
2	130.31	44.34	9.83	0.12	2	114.07	86.79	38.51	0.58
3	169.90	161.72	34.27	0.91	3	136.22	39.12	11.09	0.09
4	293.08	194.77	19.29	0.44	4	178.02	336.71	49.93	3.58
5	314.07	340.41	22.85	1.17	5	268.79	159.59	37.02	0.35
6	389.03	285.24	35.61	0.54	6	291.75	208.91	25.65	0.51
7	777.71	455.68	39.73	0.34	7	345.08	38.16	12.08	0.01
8	813.79	405.49	33.75	0.25	8	371.90	128.75	25.15	0.12
9	848.48	308.71	29.82	0.13	9	596.04	330.42	158.22	0.31
10	868.05	167.56	21.21	0.03	10	711.90	1301.58	93.62	0.18
11	883.87	106.81	13.46	0.01	11	758.39	380.56	52.19	0.25
					12	797.71	279.31	37.17	0.12
					13	837.55	212.90	34.30	0.06
					14	862.89	100.62	3.71	0.01
$\epsilon_{\infty}=2.41 \pm 0.05$ ; $\epsilon_0=7.47 \pm 0.1$					$\epsilon_{\infty}=2.26 \pm 0.05$ ; $\epsilon_0=9.52 \pm 0.1$				